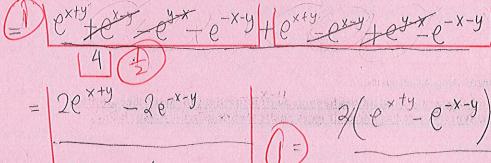
SCORE: $\frac{23}{30}$ POINTS 2 + 2

Write and <u>prove</u> a formula for sinh(x + y) in terms of sinh x, sinh y, cosh x and cosh y.

SCORE: 6 /6 PTS

$$\frac{\left(e^{x}-e^{-x}\right)\left(e^{y}+e^{-y}\right)}{2}+\frac{\left(e^{x}+e^{-x}\right)\left(e^{y}-e^{-y}\right)}{2}$$



$$= 2e^{x+y} - 2e^{-x-y}$$

$$= 2e^{x+y} - 2e^{-x-y}$$

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$$= 2e^{x+y} - 2e^{-x-y}$$

Sketch the general shape and position of the following graphs. Don't worry about specific x - or y - coordinates.

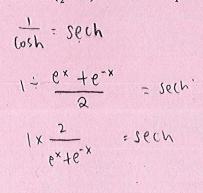
SCORE: _____/3 PTS

$$f(x) = \tanh^{-1} x$$

$$f(x) = \sinh x$$

$$f(x) = \cosh^{-1} x$$

Rewrite sech $(\frac{1}{2} \ln 3)$ in terms of exponential functions and simplify.



$$\frac{2}{e^{\frac{1}{2}\ln^3} + e^{-\frac{1}{2}\ln^3}}$$

$$= \frac{2}{e^{\frac{1}{2}\ln^3} + e^{\frac{1}{2}\ln^3}}$$

SCORE:
$$\frac{1}{2}$$
 /3 PTS
$$= 2 \div \frac{\left(e^{\frac{1}{2}\ln 3}\right)^{2} + 1}{e^{\frac{1}{2}\ln 3}}$$

$$= 2 \times \frac{e^{\frac{1}{2}\ln 3}}{\left(e^{\frac{1}{2}\ln 3}\right)^{2} + 1}$$

$$= \frac{2 \cdot e^{\frac{1}{2}\ln 3}}{\left(e^{\frac{1}{2}\ln 3}\right)^{2} + 1} = \frac{2 \cdot 3^{\frac{1}{2}}}{3^{\frac{1}{2}} + 1} = \frac{2 \cdot 3^{\frac{1}{2}}}{4}$$

Write that identity involving sinh x and cosh x. You do NOT need to prove the identity. [a]

TERM SHIP AND CHIEF PARTS ON THE

[b] Write the identity for $\cosh 2x$ that uses both $\sinh x$ and $\cosh x$ simultaneously. You do NOT need to prove the identity.

$$\int \int (\cosh^2 x + \sinh^2 x = \cosh 2x)$$

[c] Use the results of [a] and [b] to find and prove an identity for $\cosh 2x$ that uses only $\sinh x$.

$$\frac{(o\varsigma h^2 x = 1 + sinh^2 x)}{1 + sinh^2 x + sinh^2 x} = (osh 2x)$$

$$\frac{1}{1 + 2 sinh^2 x} = (osh 2x)$$

If $\tanh x = -\frac{2}{3}$, find $\sinh x$ using identities.

You must explicitly show the use of the identities but you do NOT need to prove the identities. Do NOT use inverse hyperbolic functions nor their logarithmic formulae in your solution. cosh2x - Sinh2x=1

$$\left(-\frac{2}{3}\right)^{2} + \operatorname{Sech}^{2} \times = 1$$

$$\frac{4}{9} + \operatorname{Sech}^{2} \times = 1$$

$$\operatorname{Sech}^{2} \times = \frac{9}{9} - \frac{4}{9}$$

$$\operatorname{Sech}^{2} \times = \frac{5}{9}$$

$$\frac{3nh^{2}x}{2} + \frac{9ech^{2}x}{3} = 1$$
 $\frac{4}{9} + \frac{9ech^{2}x}{3} = 1$
 $\frac{4}{9} + \frac{9ech^{2}x$

Prove that $g(x) = \ln(x + \sqrt{x^2 - 1})$ is the inverse of $f(x) = \cosh x$ by simplifying f(g(x)).

SCORE: 5 /5 PTS

You may need to use the exponential definition of cosh x.